Chapter 9: Choosing the Model (Sports Scheduling)

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- How to come up with a model for a problem
- Why choosing a good model is an art
- Channeling
- Projection
- Redundant constraints



Sports Scheduling

Tournament Planning

We plan a tournament with 8 teams, where every team plays every other team exactly once. The tournament is played on 7 days, each team playing on each day. The games are scheduled in 7 venues, and each team should play in each venue exactly once.

As part of the TV arrangements, some preassignments are done: We may either fix the game between two particular teams to a fixed day and venue, or only state that some team must play on a particular day at a given venue. The objective is to complete the schedule, so that all constraints are satisfied.

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| | Problem | | |
| | Model | | |
| | Program | | |
| | Search | | |
| | Redundant Modelling | | |
| | | | |
| Example | | | |

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

Constraint Computation

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Problem Model Program

Search Redundant Modelling

Solution

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 6, 8 | | 1, 2 | 5, 7 | | 3, 4 |
| Day 2 | 2, 3 | 1, 5 | | | 4, 8 | 6, 7 | |
| Day 3 | 1, 7 | 2, 4 | 3, 8 | | | | 5, 6 |
| Day 4 | | | 4, 7 | | 2, 6 | 3, 5 | 1, 8 |
| Day 5 | 5, 8 | | | 3, 6 | | 1, 4 | 2, 7 |
| Day 6 | | 3, 7 | 1, 6 | 4, 5 | | 2, 8 | |
| Day 7 | 4, 6 | | 2, 5 | 7, 8 | 1, 3 | | |

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| | |
| Problem | |
| Model | |

A More Abstract Formulation

Rooms Puzzle, (Thomas G. Room, 1955)

Place numbers 1 to 8 in cells so that each row and each column has each number exactly once, each cell contains either no numbers or two numbers (which must be different from each other), and each combination of two different numbers appears in exactly one cell.

Program Search

Puzzle presented by R. Finkel

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| | Problem |
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| | Model |
| | Program |
| | Search |
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How to come up with a model

- What are the variables/what are their values?
- How can we express the constraints?
- Do we have these constraints in our system?
- Does this do good propagation?
- Backtrack to earlier step as required

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| Requirements | | | | |

- There are 8 teams, seven days and seven locations
- Each team plays each other team exactly once
- Each team plays 7 games (redundant)
- Each team plays in each location exactly once
- Each team plays on each day exactly once
- A game consists of two (different) teams
- There are four games on each day (redundant)
- There are four games at each location (redundant)
- In any location there is atmost one game at a time



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Idea 1

- Matrix $Day \times Game (7 \times 4)$
- Each cell contains two variables, denoting teams
- Easy to say that team plays once on each day, alldifferent
- Columns don't have significance
- Model does not mention location, how to add this?
- How to express that each team plays each other once?

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| Idea 2, Change problem st | ructure |
| Matrix of Day × Location (7 Each cell contains two varia How do we avoid symmetry Need special value (0) to de In one cell, either both or no Easy to say that each row a exactly once | 1×7) ables, each denoting a team inside cell? enote that there is no game one of the variables are 0 and column contains each team |
| Except for value 0, can not | use alldifferent |

- Link between two variables in cell to state that game needs two different teams
- How to express that each (ordered) pair occurs exactly once?

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Idea 3, Add location variables

- Model as in Idea 1, matrix $Day \times Game$
- Each cell contains two variables for teams and one for location
- Easy to state that games on one day are in different locations
- How to express condition that each team plays in each location once?
- Also, how to express that each team plays each other exactly once?

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| Program | Comparing Ideas | | |
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| Idea 4 Use variables for nairs | | | |
| | | | |

- Matrix *Day* × *Location*
- Each cell contains one variable ranging over (sorted) pairs of teams, and special value 0 (no game)
- Each pair value occurs once, except for 0
 - Special constraint alldifferent0
 - Or use gcc
- How to state that each team plays once per day?
- How to state that each team plays in each location?



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Idea 5: If all else fails, use binary variables

- Binary variable stating that team *i* plays in location *j* at day *k*
- Three dimensional matrix
- Each team plays once on each day
- Each team plays once in each location
- Each game has two (different) teams, needs auxiliary variable
- Each pair of team meets once, needs auxiliary variables

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| Idea 6: An even bigger binary model | | | |

- Use four dimensions
- Team *i* meets team *j* in location *k* on day *l*
- 3136 = 8*8*7*7 variables
- Constraints all linear
- Why use finite domain constraints?



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Idea 7: A different mapping

- Each team plays each other exactly once, one variable for each combination (8*7/2=28 variables)
- Decide when and where this game is played, values range over combinations of days and locations (7*7=49 values)
- All variables must be different (no two games at same time and location)
- Each team plays 7 games, by construction
- How to express that each team plays once per day?
- How to express that each team plays in each location once?





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Exploring Ideas Expanding Idea 7 Comparing Ideas Channeling Selected Model

Numbering Values

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

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Four games on each day

- Day 1 corresponds to values 1..7
- Four variables can take these values
- Day 2 corresponds to values 8..14, etc
- One constraint per day
- Exactly four of all variables take their value in the set ...
- Seven such constraints

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |



Four games at each location

- City 1 corresponds to values
 - 1, 8, 15, 22, 29, 36, 43
- Four variables can take these values
- City 2 corresponds to values
 - 2, 9, 16, 23, 30, 37, 44
- One constraint per location
- Exactly four of all variables take their value in the set ...
- Seven such constraints over 28 variables each

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Problem

Program Search

Model

Exploring Ideas

Selected Model

Expanding Idea 7 Comparing Ideas

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Choosing the Model

Teams plays once on a day (at a location)

- Select those variables which correspond to Team i
- Exactly one of those variables takes its value in the set 1..7
- Same for all other days
- Same for all other teams
- 56 Constraints over 7 variables each
- Similar for teams and locations, another 56 constraints



| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

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Are we there yet?

- 28 variables with 49 possible values
- 1 alldifferent
- 7 exactly constraints over all variables (Days)
- 7 exactly constraints over all variables (Locations)
- 56 exactly constraints over 7 variables each (Days)
- 56 exactly constraints over 7 variables each (Locations)
- Forgotten anything?
- Check the requirements

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| Do we satisfy the requirements? | | |

- There are 8 teams, seven days and seven locations
- Each team plays each other team exactly once
- Each team plays 7 games (redundant)
- Each team plays in each location exactly once
- Each team plays on each day exactly once
- A game consists of two (different) teams
- There are four games on each day (redundant)
- There are four games at each location (redundant)
- In any location there is atmost one game at a time



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| Vhat about the exactly of | constraint? |

- ECLiPSe doesn't provide this constraint
 - Other system might do, could switch system
- Implement it
 - Extend gcc to allow multiple values
 - Should be last resort
- Emulate constraint with others

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| Idea 8: Mapping games to days and locations | | |

- For each game to be played, we have two variables
 - One ranges over the days
 - The other over the locations
- Easy to state that there are four games per day an location
- Easy to state that each team plays once per day and location
- How do we express that no two games are played at the same location and the same time?
 - If we had an alldifferent over pairs of variables...
 - Not in ECLiPSe



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- gcc global cardinality constraint
- Pattern is list of terms gcc(Low, High, Value)
- The overall number of variables taking value Value is between Low and High
- Generalization of alldifferent
- Domain consistent version in ECLiPSe



| Model Program Search Redundant Modelling | Expanding Ideas Expanding Ideas Comparing Ideas Channeling Selected Model | | |
|---|---|--|--|
| Each team plays once per day | | | |
| For the seven variables which | ch describe games of a team | | |

- Each row value is taken exactly once amongst the variables
- Could use gcc([gcc(1,1,1),...,gcc(1,1,7)],Vars)
- But alldifferent (Vars) is more compact
- Similar for columns

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| How do the models differ? | | |
| How do the models diller? | | |

| Idea | Mapping |
|------|--|
| 1 | $D 	imes G 	imes \{f, s\} 	o T$ |
| 2 | $D 	imes L 	imes \{f, s\} 	o T \cup \{0\}$ |
| 3 | $D 	imes G 	imes \{f, s\} 	o T$ |
| 5 | D 	imes G ightarrow L |
| 4 | $D 	imes L 	o T 	riangle T \cup \{0\}$ |
| 5 | $T \times D \times L \rightarrow \{0, 1\}$ |
| 6 | $T \times T \times D \times L \rightarrow \{0,1\}$ |
| 7 | $T \bigtriangleup T ightarrow D 	imes L$ |
| ß | $T \vartriangle T ightarrow D$ |
| 0 | $T \vartriangle T ightarrow L$ |

- D Days
- T Teams

G

- L Locations
 - Games



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Requirements Capture

| Idoa | Requirement | | | | | | | | |
|------|-------------|--------------|---|---|---|----|---|---|----|
| luca | | riequirement | | | | | | | |
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 1 | N | ? | Y | ? | Y | Y | Y | ? | ? |
| 2 | С | ? | Y | Y | Y | Y | Y | Y | Y |
| 3 | С | ? | Y | ? | Y | Y | Y | Y | Y |
| 4 | С | Y | Y | Y | Y | Y | Y | Y | Y |
| 5 | С | NL | L | L | L | NL | L | L | NL |
| 6 | С | L | L | L | L | L | L | L | L |
| 7 | С | С | С | E | E | С | E | E | A |
| 8 | С | С | С | A | A | С | G | G | ? |

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Comments on models

| Idea | Main point |
|------|--|
| 1 | missing locations, first second symmetry |
| 2 | spare value, first second symmetry |
| 3 | first second symmetry |
| 4 | spare value |
| 5 | 0/1, non-linear constraints |
| 6 | 0/1, large matrix |
| 7 | needs exactly constraint |
| 8 | needs alldifferent on tuples |



| Problem |
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| Model |
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Viewpoints and Channeling

- Instead of expressing all constraints over one set of variables
- Use multiple sets of variables (viewpoints)
- Decide which constraint to express over which variables
- Allows more freedom on how to express problem
- Link the different variables with channeling constraints



- Combine ideas 7 and 8
- One set of variables ranging over pairs
- Another using two variables per game for day and location
- How to combine variables?
- Minimize loss of information



| | Problem |
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| | Model |
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Projection

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

- Link pair variables to row and column variables
- Pair variable uses cell numbers 1-49 as values
- Row and column variables indicate on which day (row) and in which location (column) the game is played
- Pair value 23 = row 4, column 2
- element constraint to link the variables
- Two projections from $D \times L$ space onto D and L

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| Mapping cells to rows and | columns | \$ | | | | | |
| | | City 1 | City 2 City | 3 City 4 | City 5 | City 6 | City 7 |
| | | Day 1 1 | 2 3 | 4 | 5 | 6 | 7 |
| | | Day 2 8 | 16 17 | 18 | 12 | 20 | 21 |
| | | Day 4 22 | 23 24 | 25 | 26 | 27 | 28 |
| | | Day 6 36 | 37 38 | 39 | 40 | 41 | 42 |
| | l | Day 7 43 | 44 45 | 46 | 47 | 48 | 49 |
| | 1 0 0 0 0 | | 0 0 | 2 2 | 2 | 0 | |
| element(Cell,[1,1,1,1,1,1,1, | 1,2,2,2,2 | 2,2,2 | ,2,3, | 3,3 | , [,] | 3,3 | 3,3, |
| 4,4,4,4,4,4,4 | 4,5,5,5,5 | 5,5,5 | ,5,6, | 6,6 | ,6, | 6,6 | 5,6, |
| · · · · · · · · · · · · · · · · · · · | 71 Pour | | | | | • | |
| | /],KOW), | | | | | | |
| element(Cell,[1,2,3,4,5,6, | 7,1,2,3,4 | 4,5,6 | ,7,1, | 2,3 | ,4, | 5,6 | 5,7, |
| 1 2 3 4 5 6 | 71234 | 456 | 7 1 | 23 | 4 | 56 | 5 7 |
| | | 1,0,0 | , , , _ , | Z, J | / - / | 5,0 | , , |
| 1,2,3,4,5,6, | /],Col), | | | | | | |



| Problem | Exploring Ideas |
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| Model | Expanding Idea 7 |
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| Redundant Modelling | Selected Model |
| Mapping cells to rows and | columns |

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

| element(<mark>23</mark> | ,[1,1,1,1,1,1,2,2,2,2,2,2,2,3,3,3,3,3,3,3, |
|--------------------------|--|
| | 4, <mark>4</mark> ,4,4,4,4,4,5,5,5,5,5,5,5,6,6,6,6,6,6,6,6 |
| | 7,7,7,7,7,7],4), |
| element(23 | ,[1,2,3,4,5,6,7,1,2,3,4,5,6,7,1,2,3,4,5,6,7, |
| | 1, 2, 3, 4, 5, 6, 7, 1, 2, 3, 4, 5, 6, 7, 1, 2, 3, 4, 5, 6, 7, |
| | 1,2,3,4,5,6,7], <mark>2</mark>), |



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| Search | Channeling |
| Redundant Modelling | Selected Model |
| Channeling Constraints | |

Choosing the Model

- This is one common type, a projection
- Another common type is the inverse
 - Link a variable $A \rightarrow B$ to another $B \rightarrow A$

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- Typically used for bijective mappings
- Built-in inverse/2
- Also used: Boolean channeling
 - Link variables $A \rightarrow B$ and $A \times B \rightarrow \{0, 1\}$
 - Built-in bool_channeling/3



| | Problem |
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Selected Model

- Two sets of variables (Req 1, 2, 3, 6, by construction)
- Pair variables ($T \bigtriangleup T \to D \times L$)
 - alldifferent (Req 9)
- Day and Location variables ($T \bigtriangleup T \to D$), ($T \bigtriangleup T \to L$)
 - gcc (Req 4, 5)
 - alldifferent (Req 7, 8)
- Channeling Constraints
 - element projection from pairs onto rows and columns
- Search only on pair variables

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| Handling of hints (I) | | |

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

- This value (17) can not be used by pairs not involving team
 8
- One of the pairs involving team 8 must use this value (17) on straint

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Exploring Ideas Expanding Idea 7 Comparing Ideas Channeling Selected Model

Handling of hints (II)

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

• The pair involving teams 5 and 7 must take value 5, fixes variable

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hint(1,8,[2-[8],5-[5,7],8-[2],9-[1,5],15-[7], 17-[8],26-[2],27-[5],28-[1],29-[8], 34-[1],39-[4,5],43-[4],47-[1,3]]).



Main Program



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Main Program (continued)

```
project_row_cols(L,N1,Rows,Cols),
limit (Rows, N2, N1),
limit(Cols,N2,N1),
separate(Contains, Rows, N, SplitRows),
separate(Contains, Cols, N, SplitCols),
(foreach(K, SplitRows) do
    ic_global_gac:alldifferent(K)
),
(foreach(K, SplitCols) do
    ic_global_gac:alldifferent(K)
),
search(L,0,input_order,indomain,
       complete, []).
```

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Create Pairs and Names

```
create_pairs(N, Contains, Names):-
     (for(I, 1, N-1)),
      fromto(Names, A1, A, []),
      fromto(Contains, B1, B, []),
     param(N) do
          (for(J,I+1,N)),
           fromto(A1, [Name|AA], AA, A),
           fromto(B1,[I-J|BB],BB,B),
          param(I) do
              concat_string([I,J],Name)
         )
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    ).
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```

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```
project_row_cols(L,N,Rows,Cols):-
  generate_tables(N,RowTable,ColTable),
  (foreach(X,L),
    foreach(R,Rows),
    foreach(C,Cols),
    param(RowTable,ColTable) do
       element(X,RowTable,R),
       element(X,ColTable,C)
).
```



Generating Projection Tables

```
generate_tables(N,RowTable,ColTable):-
     (for(I,1,N),
      fromto(RowTable, A1, A, []),
      fromto(ColTable, B1, B, []),
     param(N) do
         (for(J,1,N),
          fromto(A1,[I|AA],AA,A),
          fromto(B1,[J|BB],BB,B),
          param(I) do
              true
         )
                                                         ork
                                                      onstraint
    ).
                                                      omputation
                                                        Centre
```

Choosing the Model



Helmut Simonis

```
separate(Contains, Rows, Values, SplitRows):-
     (for (Value, 1, Values),
     foreach(SplitRow, SplitRows),
     param(Contains, Rows) do
         (foreach (A-B, Contains), foreach (V, Rows),
          fromto([],R,R1,SplitRow),param(Value) do
              (memberchk(Value, [A, B]) ->
                  R1 = [V|R]
              ï
                  R1 = R
              )
                                                         Cork
         )
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                                                      omputation
    ).
                                                        Centre
```



```
limit(L,Bound,Values):-
  (for(I,1,Values),
    foreach(gcc(Bound,Bound,I),Pattern),
    param(Bound) do
        true
  ),
  gcc(Pattern,L).
```



```
process_hints(L,Contains,Hints):-
   (foreach(Pos-Values,Hints),
    param(L,Contains) do
        process_hint(Pos,Values,L,Contains)
   ).
process_hint(Pos,[A,B],L,Contains):- % clause 1
   !,
   match_hint(A-B,Contains,L,X),
   X #= Pos.
```

Cork onstraint omputation Centre

Problem Model Program Search Redundant Modelling Setting up hints



| Problem Model Program Search Redundant Modelling | |
|---|--|
| Setting up hints | |

```
not_mentioned(A, B, V):-
    A \= V,
    B \= V.
match_hint(H, [H|_], [X|_], X):-
    !.
match_hint(H, [_|T], [_|R], X):-
    match_hint(H, T, R, X).
```





Choosing the Model

Using input order

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | 1 |
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Helmut Simonis

Redundant Modelling

Solution

Problem

Program Search



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Using input order First Fail Strategy

Redundant Modelling

Search Tree with input order



| Problem Model Program Search Redundant Modelling | Using input order First Fail Strategy |
|---|--|
| How to improve? | |

- Try different search strategy
- Use first_fail dynamic variable selection



| Problem Model Program Search Redundant Modelling | Using input order First Fail Strategy |
|---|--|
| Search Tree with first fail | |
| | 31 34 |

| Helmut Simonis | Choosing the Model | 57 |
|---|--|----|
| | | |
| Problem Model Program Search Redundant Modelling | Using input order First Fail Strategy | |
| Observation | | |

8 12 16

- It does not work
- Search tree is slightly larger than before!



Constraint computation centre

Problem Model Program Search Adding *value index* Channeling Improving Handling of Hints

Missing Propagation

| | 0.1 | 0.1 | 0.1 0 | 0.1 | 0.1 | 0.1 | 0.1 7 |
|---------|--------|--------|--------|--------|--------|--------|--------|
| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

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Redundant Modelling

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

Constraint Computation Centre

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Choosing the Model

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Problem Model Program Search Redundant Modelling

Adding *value index* Channeling Improving Handling of Hints

Missing Propagation

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |





Problem Model Adding value index Channeling Program Search

Redundant Modelling

Missing Propagation

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

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| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

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Choosing the Model

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Problem Program Search Redundant Modelling

Adding value index Channeling

Missing Propagation

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
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| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |







Adding *value index* Channeling Improving Handling of Hints

Missing Propagation

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
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| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

Cork Constraint Computation Centre

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Choosing the Model

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Problem Model Program Search Redundant Modelling

Adding *value index* Channeling Improving Handling of Hints

Missing Propagation

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
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| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
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| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
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Problem Model Program Search

Redundant Modelling

Adding value index Channeling Improving Handling of Hints

Missing Propagation

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

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| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
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| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

ork onstraint omputation Centre

65

| ſ | Problem Model Program Search Redundant Modelling | Adding <i>value index</i> Channeling Improving Handling of Hints | |
|--------------|--|---|--|
| Why is this? | | | |

Choosing the Model

Helmut Simonis

- Constraints involved:
 - gcc constraint on row: four variables can use values from this row
 - four occurrence constraints for hints: One of the variables must take this value
- No interaction between constraints, only between constraints and variables
- We do not detect that value 1 can not be used
- Eventual solution respects condition, model is correct
- We are concerned about propagation, not just correctness Cork

onstraint omputation Centre

| Redundant Modelling |
|---------------------|
| Search |
| Program |
| Model |
| Problem |

Adding *value index* Channeling Improving Handling of Hints

Adding Redundant Constraints

- Add constraints which do more propagation, but do not affect solutions
- Lead to smaller search tree, hopefully faster solution
- Introduction requires understanding of (lack of) propagation
- Visualization is key to detect missing propagation



- Day × Location matrix of 0/1 variables
- Indicates if there is a game on this day at this location
- Row/column sums: 4 games in each row/column
- Hint given for cell: Game variable is 1



Problem

Adding *value index* Channeling Improving Handling of Hints

Channeling Constraint

- Link pair variables P_i to 0/1 variables Y_i as value-index
- $(\exists i \text{ s.t. } P_i = v) \Leftrightarrow Y_v = 1$
- Propagation:
 - $P_i = v \Rightarrow Y_v = 1$
 - $Y_v = 0 \Rightarrow \forall i : P_i \neq v$
 - $(\forall i: v \notin d(P_i)) \Rightarrow Y_v = 0$
 - $Y_v = 1 \Rightarrow \text{occurrence}(V, P_1...P_n, N), N \ge 1$

| | | Computation Centre |
|--|---|-----------------------|
| Helmut Simonis | Choosing the Model | 69 |
| | | |
| Problem Model Program Search Redundant Modelling | Adding <i>value index</i> Channeling Improving Handling of Hints | |
| Added Program | | |
| <pre>value_set_channeling(L,F dim(Matrix,[7,7]), Matrix[17,17] :</pre> | Hints):- : 01, | |
| flatten_array(Matrix | , x,ValueSet), | |

- value_set_channel(L,ValueSet,1),
 - (for(I,1,7),param(Matrix) do
 sumlist(Matrix[I,1..7],4),
 - sumlist(Matrix[1..7,I],4)
 -), (foreach(K-_,Hints),param(Matrix) do coor(K,I,J), subscript(Matrix,[I,J],1)

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Adding *value index* Channeling Improving Handling of Hints

Before Search





| Helmut Simonis | Choosing the Model | 71 |
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| Problem | | |
| Model | Adding value index Channeling | |
| Program | Improving Handling of Hints | |

Search

Redundant Modelling

Impact of Redundant Constraints



With value index channeling





Adding *value index* Channeling Improving Handling of Hints

Solution





| Helmut Simonis | Choosing the Model | 73 |
|---------------------------------------|---|----|
| | | |
| | | |
| Problem Model Program Search | Adding <i>value index</i> Channeling Improving Handling of Hints | |
| Redundant Modelling | | |

Search Tree



Constraint Computation Computation

Adding *value index* Channeling Improving Handling of Hints

Still Missing Propagation

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |



| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
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| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

Game 12 can not be played on day 1 at locations 5 or 6



Helmut Simonis Choosing the

Choosing the Model

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Problem Model Program Search Redundant Modelling

Adding *value index* Channeling Improving Handling of Hints

Still Missing Propagation

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 City 4
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 Day 1
 8
 7,5

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
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| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| Day 3 | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

Game 12 can not be played on day 1 at locations 5 or 6



Improving Handling of Hints

Still Missing Propagation

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |



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| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
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Game 12 can not be played on day 1 at locations 5 or 6



Helmut Simonis

Choosing the Model

Problem Program Search Redundant Modelling

Adding value index Channeling Improving Handling of Hints

Still Missing Propagation



City 5 City 6 City 7 7, 5 City 2 City 3 City 4 8 City 4 City 1 Day 1 1, 5 Day 2 Day 3 7 8 Day 4 Day 5 8 5, 4 Day 6 4 1, 3 Day 7

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
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Improving Handling of Hints

Still Missing Propagation

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|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
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| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
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| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| Day 2 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
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| Day 4 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| Day 5 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

Game 12 can not be played on day 1 at locations 5 or 6



Helmut Simonis

Choosing the Model

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Problem Program Redundant Modelling

Improving Handling of Hints

Still Missing Propagation

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| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
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| Day 1 | | 8 | | | 7, 5 | | |
| Day 2 | 2 | 1, 5 | | | | | |
| Day 3 | 7 | | 8 | | | | |
| Day 4 | | | | | 2 | 5 | 1 |
| Day 5 | 8 | | | | | 1 | |
| Day 6 | | | | 5, 4 | | | |
| Day 7 | 4 | | | | 1, 3 | | |

| | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 |
|-------|--------|--------|--------|--------|--------|--------|--------|
| Day 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
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| Day 6 | 36 | 37 | 38 | 39 | 40 | 41 | 42 |
| Day 7 | 43 | 44 | 45 | 46 | 47 | 48 | 49 |

Game 12 can not be played on day 1 at locations 5 or 6



| Problem | |
|----------------------------|--|
| Model | |
| Program | |
| Search | |
| Redundant Modelling | |

Adding *value index* Channeling Improving Handling of Hints

Our model does not deal well with hints

- Preset game is ok, leads to variable assignment
- Preset team is weak, adds new constraint
- As there is no interaction of this constraint with the other constraints, there is no initial domain restriction
- Model is correct, but lazy

| | | | | | | | | Constraint Computation Centre | | | |
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| | | | Helmut | t Simonis | Choosing the Model 8 | | | | | | |
| | | | | | | | | | | | |
| | | | Redundant | Problem Model Program Search Modelling | Adding <i>value index</i> Channeling Improving Handling of Hints | | | | | | |
| Second Attempt: Improving the handling of hints | | | | | | | | | | | |
| | | | | | | | | | | | |
| Γ | | City 1 | City 2 | City 3 | City 4 | City 5 | City 6 | City 7 | | | |
| | Day 1 | | 8 | | | 7, 5 | | | | | |
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| | Day 5 | 8 | | | | | 1 | | | | |
| | Day 6 | | | | 5, 4 | | | | | | |
| | Day 7 | 4 | | | | 1, 3 | | | | | |

- This value can not be used by pairs not involving team 8
- One of the pairs involving team 8 must use this value
- These values can not be used by any pair involving team computation

oputation

| Model Program Search Model Adding <i>value index</i> Channeling Improving Handling of Hints |
|--|
| Redundant Modelling |
| Redundant Constraints |
| Red value can not be used by pairs not involving team 8 disequalities One of the pairs involving team 8 must use red value |
| Occurrences(gcc) constraint Vellow velues can not be used by any pair involving team 9 |
| Yellow values can not be used by any pair involving team 8 disogualities |
| City 1 City 2 City 3 City 4 City 5 City 7 Day 1 8 7,5 1 Day 2 1,5 1 1 Day 4 2 5 1 Day 6 5,4 1 1 Day 7 4 1,3 1 Computation (Computation (Com |
| Helmut SimonisChoosing the Model83 |
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| Problem Model Model Program Search Improving Handling of Hints Added Program Search Redundant Modelling Adding value index Channeling |
| <pre>improved_hint(Pos,[Value],L,Contains):- (foreach(X,L),foreach(A-B,Contains), fromto([],R,R1,Required), param(Pos,Value) do (not_mentioned(A,B,Value) -></pre> |
| occurrences(Pos,Required,1), |
| excluded_locations(Pos,Excluded), |

Problem

exclude_values(Required,Excluded).

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Added Program



Improving Handling of Hints

Problem Model Program

Search

Redundant Modelling



```
...
(for(J,1,7),
fromto(E1,A,A1,Excluded),
param(X,Pos) do
    coor(K,X,J),
    (Pos = K ->
        A1 = A
    ;
        A1 = [K|A]
    )
).
```



| Model Program Search Redundant Modelling | Adding <i>value index</i> Channeling Improving Handling of Hints | |
|--|---|---|
| Added Program | | |
| | | |
| | | |
| <pre>exclude_values(Vars,Valu (foreach(X,Vars), param(Values) do (foreach(Value,V param(X) do X #\= Value)).</pre> | ues):- Values), | |
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Adding *value index* Channeling Improving Handling of Hints

Before Search







Problem Model Program

- We don't need the value index channeling
- It is subsumed by the improved hint treatment
- Always worthwhile to check if constraints are still required after modifying model



Conclusions

• Many ways of modelling even simple problems

Conclusions Exercises

- Selection of "best" model difficult
 - Depends on constraints available
 - Often needs experimentation
- How do we measure if one model is "better" than another?
 - Execution time?
 - Size of search tree?
 - Scalability?
- Definition of variables is key
- Explore choices by considering mapping operators



- Channeling Combining viewpoints
 - Express some constraints in one, others in second viewpoint
 - Channeling constraints to link the viewpoints
 - Decide which model to use for search
- Redundant Constraints Improving constraint propagation
 - Constraints are logically implied by other constraints
 - Provide more propagation to reduce search space



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Modelling for Constraint Programming.

ACP Summerschool 2008, St Andrews, Scotland, 2008.

http://www-circa.mcs.st-and.ac.uk/cpss2008/slides/ SmithSummerSchool1.pdf http://www-circa.mcs.st-and.ac.uk/cpss2008/slides/ SmithSummerSchool2.pdf http://www-circa.mcs.st-and.ac.uk/cpss2008/slides/ SmithSummerSchool3.pdf http://www-circa.mcs.st-and.ac.uk/cpss2008/slides/ SmithSummerSchool4.pdf

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viewpoint, and how to link the views together?

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Choosing the Model